

Math 31
Rationals

Name Key
Date _____

→ cause ÷ zero

1. Identify the non-permissible values and simplify both the following.

a) $\frac{(2x+3)(x+4)}{(x-4)(2x+3)}$

$x \neq 4$

$x \neq -\frac{3}{2}$

b) $\frac{x^2 + x - 20}{x^2 - 25}$

$= \frac{(x+5)(x-4)}{(x+5)(x-5)}$

$\frac{(x+5)(x-4)}{(x+5)(x-5)}$

$x \neq 5 \quad x \neq -5$

2. Simplify the following expressions.

a) $\frac{6x+9}{x^2+3x} \div \frac{12x^2+18x}{12x+4x^2}$

$= \frac{3(2x+3)}{x(x+3)} \times \frac{4x(3+x)}{6x(2x+3)}$

$= \frac{(3)(4x)}{(x)(6x)}$

$= \frac{2}{x}$

b) $\frac{2x^2+11x+15}{x^2+2x-3} \times \frac{x^2-3x+2}{4x^2+8x-5}$

+6, +5 *-2, -1*
+3, -1 *+10, -2*

$= \frac{(2x+5)(x+3)}{(x+3)(x-1)} \cdot \frac{(x-2)(x-1)}{(2x+5)(2x-1)}$

$= \frac{x-2}{2x-1}$

3. Simplify the following expressions. ↗ common denominator

$$\frac{3}{5} \left[\frac{x+5}{4} + \frac{x+2}{6} \right] \frac{2}{2}$$

$$= \frac{3x+15}{12} + \frac{2x+4}{12}$$

$$= \frac{5x+19}{12}$$

$$\frac{(x+3) \frac{x+1}{5} - \frac{x+2}{x+3} \left(\frac{5}{5}\right)}{(x+3)}$$

$$= \frac{x^2+x+3x+3}{5(x+3)} - \frac{5x+10}{5(x+3)}$$

$$= \frac{x^2+4x+3-5x-10}{5(x+3)}$$

$$= \frac{x^2-x-7}{5(x+3)}$$

4. Solve.

quad=0
(f₁)(f₂)=0

a) $\left[x - \frac{7}{2} = \frac{2}{x} \right] 2x$

$$2x^2 - 7x = 4$$

$$2x^2 - 7x - 4 = 0$$

$$(2x+1)(x-4) = 0$$

$$2x+1=0 \quad x-4=0$$

$$x = -\frac{1}{2} \quad x = 4$$

b) $\left[x - \frac{8}{x+5} = 4 \right] x+5$

$$x^2 + 5x - 8 = 4x + 20$$

$$x^2 + x - 28 = 0$$

$$x = \frac{-1 \pm \sqrt{(1)^2 - 4(1)(-28)}}{2(1)}$$

$$x = \frac{-1 \pm \sqrt{113}}{2}$$